

TAX REFORM IN TUNISIA: A SIMULATION BASED ANALYSIS USING THE NEW AREA-WIDE MODEL

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Abstract

This paper aims to modeling an emergent economy like Tunisia which is rarely used when calibrating the New Area-Wide Model. Indeed, some modifications and features are introduced for the calibration of a small open economy of an emergent market. For instance the presence of the non-Ricardian agents as a financial fraction that is very important when gauging the impact of tax reform, the wage heterogeneity in the labor market and the risk premia in the budget constraint. To perform a tax reform, this paper tests the long-run effects of a number of fiscal consolidation scenarios based on a revenue and expenditure side on the key macroeconomic aggregates and simulates the economic activity. We discover that the fiscal consolidation strategy based on the revenue side when lowering distortionary taxes has a positive long-run effect on the output. Contrariwise, the consolidation strategies based on the expenditure side has a negative long run impact on the output, but replicates an increase in the household's wages as well as the consumption and the investment. The model is calibrated on the Tunisian economy using an annual data over 1980–2011.

Keywords: Tax reform, fiscal policy, DSGE modeling, fiscal consolidation, Tunisia, heterogeneous agent

INTRODUCTION

The recent economic and financial crisis in Europe and in Tunisia urged the government to put in place an ambitious fiscal stimulus plans as well as many fiscal policy consolidation strategies. The fiscal system in Tunisia has suffered from many diseases. For example we note the budget deficit which is above 7% of GDP that surpasses the international norm (3%), the explosion of public debt which amount to 36.616 billion TND in 2013 so 47.2% of the GDP, the increase of the State's expenditure so that the budget was 17.884 billion TND in 2010 and rise to 28.125 billion TND in 2014. Also we note the fiscal injustice where the tax burden, supported especially by employees is far superior to the other classes of society. According to Jlassi (2013) there is no an interesting measure to fight against tax evasion and the informal market. In this context, Nabli (2013), the past Governor of Central Bank of Tunisia, emphasized "The fiscal policy is not taking robust decision concerning the public investment" In fact the implementation of a large-scale fiscal spending programs and a tax reform in Tunisia and around the world sparked a vigorous policy debate. Fiscal authorities mainly have the possibility of increasing or decreasing taxes and/or cutting or increasing public spending. What are the expected consequences from these measures on the output, the consumption and the investment in the short and the long run? In this case, the choice of the New Area Wide Model (NAWM) presented by Coenen et al. (2008) and Christoffel et al. (2008) referred to as CMS and CCW respectively, is proposed as a new tool of modeling. The later is a class of the dynamic stochastic general equilibrium model (DSGE) employed for developing micro-founded DSGE models. It is a two-country open-economy model developed at the European Central Bank (ECB's) for the fiscal policy simulation. In fact, it is chosen because it included many characteristics. First it has a rich set of distortionary taxes like taxes on consumption purchases, labor and capital income, as well as profits, so that many fiscal policies instruments can be analyzed. Second it is suitable for the quantitative policy analysis, forecasting and assessing the macroeconomic effects of the alternative fiscal consolidation strategies as well as the distributional effects of many shocks in small or large countries. Third the NAWM enables us to better understand the impact of a tax reforms on the labour-market and the economic performance. Fourth it incorporates numerous nominal, real rigidities and real frictions empirically significant like the sticky prices and wages, the habit persistence in consumption, the investment adjustment cost, the international financial linkages, besides the financial frictions that is the fraction of liquidity constrained household. In this perspective Mertens and Ravn (2011) reported that such frictions dampens the short-run response of output, consumption, investment and hours of work to unanticipated tax changes and ameliorate the model's quantitative performance. It is interesting to compare between Tunisia and Euro Area

in terms of the national tax structures given its significant factor in explaining the differences in the labor utilisation and the economic performance. In fact the tax wedges in Tunisia is higher than in Euro Area. As the overall tax wedge in Tunisia amounts to roughly 74.3 % of the earnings of an average production worker, while that in the Euro Area is about 64%. Thus Tunisia has an overall tax wedge about 10% points higher than that of Euro Area.

One of the important contributions of this paper is to use this model in an emergent countries viz. Tunisia and to fit the model with the data. Indeed the model is frequently used in Euro Area, rarely used in Emergent Asia and Brazil (see Jacquinot and Straub (2008); De Carvalho and Valli (2011) whereas it seems to be the first one to my best knowledge to be applied in Tunisia. It is worth noticing that there are some differences from the CMS model considered as a contribution to the literature of the medium-scale (DSGE) models for the fiscal policy analysis. First the labor market is augmented by introducing the heterogeneity in labor skill to allow wage heterogeneity amongst the households that supply the same amount of worked hour. In this perspective, Valli and De Carvalho (2010) précised that this heterogeneity within the household generates an important differences in the impulses responses of the model compared to CMS. Second the recursive form of the optimal wage setting as well as the wage dispersion indices 's degree and the demand function for labor I and J, are corrected relating to the version of CMS. Third, the risk premia is added in the budget constraint. Ultimately, the modeling of the domestic economy's monetary authority with the traditional Taylor forward looking rule includes an expectations scheme of the inflation to better approximate the conduct of the policy to an inflation targeting framework as picked up by Ben Chalbia (2010). With regards to the literature, there are an extensive existing literature exploring the effect of fiscal consolidations on macroeconomic aggregates, especially the consumption and the output. For instance, Coenen et al. (2012) who examined seven structural DSGE models used by policymaking institution exposed to a discretionary fiscal stimulus shocks using seven different fiscal instruments. Also Coenen et al. (2008) who evaluated the macroeconomic effects of an alternative fiscal consolidation policies as a permanent reduction in the targeted government debt-to-output ratio in the NAWM model. This strand of literature is also pursued by Kitao (2010) who described the temporary tax-cut and a rebate transfer to stimulate the economic activities. Eventually, De Carvalho and Valli (2011) who modeled a fiscal policy that pursues primary surplus targets to stabilize the debt-to-GDP ratio in Brazil and explored some of the implications of the fiscal policy with the NAWM. It is worth noting that the main objective of this paper is to evaluate the benefits and the spillovers of reducing the taxes using two major government revenue components which are the income taxes, as well as the indirect taxes on the consumption goods. Beginning by the expenditure fiscal side, the transitional effects of the

monetary and government spending shock will drive down the output in the medium and the long run while the transfer shock will push up the output in the medium run. For the fiscal revenue side, the strategy based on lowering distortionary taxes, leads to an expansion of the output in the long run. However, the result differs in terms of consumption as it decelerates in the long run when reducing the consumption taxes and rises when reducing labor taxes. Likewise Papageorgiou (2012), it is discovered that the policy instrument followed by the reduction in the consumption tax rate causes a fall in the output which will recover in the long run. Furthermore, the existence of heterogeneous household makes important the distributional effects of the fiscal consolidation (Coenen et al. 2008). The paper is outlined as follows, sections 2 illustrates the specification of the NAWM model focusing on the extension proposed, section 3 provides details about the calibration strategy and performs a dynamic simulation. Section 4 experiments different fiscal consolidation strategies and analyses the dynamic responses of the model as well as the distributional effects under many shocks. Finally, section 5 concludes.

THE MODEL

The model following the spirit of (Coenen et al, 2008), consists of two economies of a different population size s and $s-1$. The novelty in this context is to introduce the Tunisian economy, which is an emergent country, proposed as a home economy and consider the Euro Area as a foreign economy. The foreign economy is modeled exactly in the same spirit as the CMS model. There is an international linkage from the trade of goods and international assets financial markets, enabling imperfect exchange-rate pass-through to consumer prices and financial intermediation costs leading to the imperfect risk sharing. In every country of the NAWM model, there are four types of the economic agents: the households, the firms, the fiscal and the monetary authority. It is assumed that the domestic economy is represented by a continuum of households grouped into two sets I and J. The members of household I are indexed by $i \in [0, 1-\omega]$ while the others are indexed by $j \in [1-\omega, 1]$. The first type of household J are called the constrained household or the non ricardian agents. They holds only their labor income, cannot trade in the financial and physical assets, and have no access to the capital markets and investment choices. The latter differ in terms of their labor skills. Nevertheless, the household I are called “non constrained” or “ricardian households. They maximize their lifetime intertemporal utility by choosing the consumption good $C_{i,t}$ and the labor services $N_{i,t}$ so they rent services to firms. They also choose the private investment good $I_{i,t}$ to purchase, which is linked to the next period physical private capital stock $K_{i,t+1}$, the intensity of capital

utilization u_{it} in production. They accumulate physical capital; have access to financial markets, where they trade domestic government bonds of the next period $B_{i,t+1}$ and internationally or private foreign bonds $B_{i,t+1}^F$. They also hold money for $M_{i,t}$ for transaction purposes, are with better labor skills and have full access to savings technologies. Thus the utility function is defined as follows:

$$E_t \left[\sum_{k=0}^{\infty} \beta^k \left(\frac{1}{1-\sigma} (C_{i,t+k-1} - \kappa C_{i,t+k-1})^{1-\sigma} \frac{1}{1+\zeta} (N_{i,t+k})^{1+\zeta} \right) \right] \quad (1)$$

In this case β denotes the intertemporal discount factor, σ is the inverse of the intertemporal elasticity of consumption substitution, ζ is the inverse of the labor effort's elasticity relative to the real wage or the Frisch elasticity of labor supply, κ is the external habit persistence or the habit formation in consumption. This function is subject to the period by period budget constraint :

$$(1 + \tau_t^c + \Gamma_v v_{i,t}) P_{c,t} C_{i,t} + P_{l,t} I_{i,t} + R_t^{-1} B_{i,t+1} + ((1 - \Gamma_{B^F}(B_t^F)) \eta P_{R,t})^{-1} S_t B_{i,t+1}^F + M_{i,t} + \Xi_{i,t} + \phi_{i,t} = (1 - \tau_t^N - \tau_t^{wh}) W_{i,t} N_{i,t} + (1 - \tau_t^k) (R_t^k u_{i,t} - \Gamma_u(u_{i,t}) P_{l,t}) K_{i,t} + \tau_t^K \delta P_{l,t} K_{i,t} + (1 - \tau_t^D) D_{i,t} + TR_{i,t} - T_{i,t} + B_{i,t} + S_t B_{i,t}^F + M_{i,t-1} \quad (2)$$

The steady state spread η^P between the interest rates of foreign and domestic bonds is considered essential in the emergent countries such as Brazil or Tunisia. In fact this risk premia, is included in the budget constraint of the household I, as As the spirit of De Carvalho and Valli (2011), in order to take in consideration the fact that the real interest rates in Tunisia are substantially higher than in the developed world even in the steady state. Then, S_t is considered as the nominal exchange rate expressed in terms of units of the home currency per unit of foreign currency. R_t and $R_{F,t}$ are respectively the riskless free returns or the interest rate on the domestic government bonds and the foreign bonds. $\Gamma_{B^F}(B_t^F)$ is the financial intermediation premium that the household member I should pay on their international debt when the external debt deviates from the steady state in the international market. $\Xi_{i,t}$ is the incurred foreign risk intermediation premium rebated in a lump-sum manner in the negotiation of the international bonds. When $\gamma_B^F > 0$, the domestic household members do not hold internationally traded bonds and the net foreign asset position is zero worldwide in the stochastic steady state. $\Gamma_v(v_{i,t})$ is the technology transaction cost on the purchase of the consumption good. This cost is linked to the inverse of the household member's money-to-consumption ratio $v_{i,t}$ and to $\gamma_v, 1, \gamma_v, 2 > 0$ (Schmitt-Grohe and Uribe, 2007) and is identical across both types of

households. The household member l hold the stock of contingent securities $\phi_{i,t}$. This latter acts as an insurance against the risks on the labor income or the wage income traded amongst all members of these households. Concerning the earning side, $W_{i,t}$ is the wage earned by household i for the unit of the labor services $N_{i,t}$. $P_{c,t}$ and $P_{I,t}$ are respectively the price of a unit private final consumption and the investment good. $R_{k,t}$ is the rate of return on the private capital services rented to firms. $TR_{i,t}$ is the transfer's payment from the government. $D_{i,t}$ is the dividend paid by the household-member-owned firms. To finance its expenditure, the fiscal authority takes part of the gross income of the household. It imposes the taxes on different sources of the income like the wage income $W_{i,t}N_{i,t}$, the capital income $R_{k,t}^K K_{i,t}$, the consumption purchases and the dividend $D_{i,t}$ income. Where τ_i^c is the tax imposed on the consumption purchase, τ_i^N is the labor income taxes, τ_i^D is the taxes on dividend, τ_i^{wh} is the household's contribution to social security imposed on the wage income, τ_i^{wh} is the tax rate representing the firm's contribution to social security, τ_i^K is the capital income taxes, $T_{i,t}$ is a lump sum only paid for the foreign economy. This instrument is chosen to stabilize the debt-to-GDP ratio (De Carvalho and Valli, 2011). It depends on the fiscal authority's target for the ratio of government debt to output. The capital accumulation owned by the household l depends on the generalized adjustment cost of investment $\Gamma(I_{i,t}/I_{i,t-1})$. The latter is formulated in terms of changes in the investment which hinge on the parameter of investment adjustment cost function γ_I and the depreciation rate δ . For its part, the capital utilization cost $\Gamma_u(u_{i,t})$ relies on varying the intensity of utilizing the physical capital stock from the steady state $u_{i,t}$ and the capital utilization cost function parameters $\gamma_{u,1}$, $\gamma_{u,2} > 0$. Also it is assumed that both types of the households act as wage setters in monopolistic competitive labor markets. As a consequence, they supply sufficient differentiated labor services to firms to satisfy the labor demand. The wages setting $W_{i,t}$ are characterized by sticky nominal wages set à la Calvo (1983). The household can optimally reset their nominal wage contract with probability $1 - \xi$ of optimizing each period t . The latter choose the same wage rate $\tilde{W}_{l,t} = \tilde{W}_{i,t}$ as well as the indexation resulting in two separate wages Phillips curves. $\tilde{W}_{l,t}$ is the optimal wage contract chosen by the household l receiving the permission to reset their wage in period t . These households are supposed to maximize the lifetime utility, as defined by equation (1). The other households who cannot optimize, readjust their wages $W_{i,t}$ based on a geometric average of past changes in the price of the private consumption good $P_{c,t}$ and the steady state consumer inflation rate π_c with λ_I the weight of past

inflation. The aggregate wage is based on the two previous equation of the wage setting so that he wage index $W_{I,t}$ evolves according to:

$$W_{I,t} = ((1 - \xi_I)(\tilde{W}_{I,t})^{1-\eta_I} + \xi_I \left(\frac{P_{C,t-1}}{P_{C,t-2}} \right)^{\chi_I} \pi_C^{1-\chi_I} W_{I,t-1})^{1-\eta_I} \chi_I^{-1} \quad (3)$$

The same reasoning holds for the household J. Turning to the firms, there are two types of firms in the productive sector of the economy indexed by $f \in [0,1]$. They operate under monopolistic competition with Calvo-type price rigidities. The first one produces the intermediate tradable goods $Y_{f,t}$ sold in the domestic market. The second set, produces the non tradable final goods like the private consumption Q_t^C , the private investment Q_t^I and the public consumption good Q_t^G . The Final goods firms are assumed to operate under imperfect competition. They combine the imported with the domestic intermediate goods in their purchases. The intermediate good firm's f produces its intermediate good output $Y_{f,t}$ in the competitive markets, with the increasing- returns-to-scale Cobb-Douglas technology, using the homogenous capital services, $K_{f,t}$, rented from the household I as input as well as the index of labor services $N_{f,t}$ yielding a technology constraint :

$$Y_{f,t} = \max[z_t K_{f,t}^\alpha N_{f,t}^{1-\alpha} - \psi, 0] \quad (4)$$

Where ψ is the share of fixed cost in production. z_t is the steady state level of productivity or the total factor productivity assumed to be identical across firms. It evolves over time according to serially correlated process. In this case ρ_z is the autoregressive coefficient of productivity and $\varepsilon_{z,t}$ is a white noise shock to productivity. Since all the firms f face the same input prices and have access to the same production technology , the nominal marginal cost $MC_{f,t}$ is identical across firms that is $MC_{f,t} = MC_t$. To adapt this model to the emergent country, we follow the approach of Fabia and De Carvalho (2010) and assume that the firms rent labor with unequal labor skills and that the individual with lower level of labor skills are more constrained on their investment possibilities and has lower level of education. This strategy of modeling enable a steady state where skillful workers earn more yet while working the same hours as the less skilled one. In Tunisia the labor contracts require 8 hour work day. The labor input used by firms f to produce the labor output $N_{f,t}$ is given by:

$$N_{f,t} = ((1 - v\omega)^{\frac{1}{\eta}} (N_{f,t}^I)^{1-\frac{1}{\eta}} + (v\omega)^{\frac{1}{\eta}} (N_{f,t}^J)^{1-\frac{1}{\eta}})^{\frac{\eta}{\eta-1}} \quad (5)$$

Where ω is the population size adjustment to the firm's labor demand and the parameter $\nu \in [0, 1/\omega]$ is added to introduce a bias in favor of a more skilled worker. When $\nu = 1$ this means that there are equally skilled workers. The parameter $\eta > 1$ denotes a price elasticity to demand for a specific labor bundles between two households. $N_{f,t}^I$ and $N_{f,t}^J$ are expressed in terms of the intratemporal elasticity of substitution between the differentiated labor services η_I and η_J of the household I and J. Firms choose the quantity required to hire in both groups of households by taking average wages $W_{I,t}$ and $W_{J,t}$ and minimizing total labor cost $N_{f,t}^I W_{I,t} + N_{f,t}^J W_{J,t}$ subject to $N_{f,t}^J$. It yields from the first order condition the aggregate wage index given by:

$$W_t = ((1 - \nu\omega)(W_{I,t})^{1-\eta} + \nu\omega(W_{J,t})^{1-\eta})^{1/\eta} \quad (6)$$

In this case $W_{I,t}$ and $W_{J,t}$ are the nominal wage indexes for the household I and J. While the aggregate demand functions for the labor of each group of households J and I are expressed as follow:

$$N_{f,t}^J = \nu\omega \left(\frac{W_{J,t}}{W_t} \right)^{-\eta} N_{f,t} \quad (7)$$

$$N_{f,t}^I = (1 - \nu\omega) \left(\frac{W_{I,t}}{W_t} \right)^{-\eta} N_{f,t} \quad (8)$$

As for the households, when taking into account the price setting, each intermediate firms charges different prices at home and sell its differentiated output $Y_{f,t}$ in both domestic and foreign market under monopolistic competition with calvo price rigidities. Firm f receive permission to set optimally prices $P_{H,f,t}$ and $P_{X,f,t}$ in a given period t with a probability of not optimizing ξ_H or ξ_X .

However, the firms which are not allowed to optimize their price, adjust their price in the domestic and foreign market such that the price contracts $P_{H,f,t}$ and $P_{X,f,t}$ are indexed to a geometric average of the past intermediate good inflation. Where $P_{H,t}$ and $P_{X,t}$ are the price indexes and χ_H and χ_X are the indexation parameter determining the weight on the past inflation. More precisely χ_H is the degree of domestic price of home good indexation and χ_X is the degree of foreign price of home good indexation (export good). π_H and π_X are the domestic and foreign intermediate goods' steady state inflation rates.

After aggregating over firms the aggregate price index $P_{H,t}$ set by the intermediate good firms for the domestically sold product evolves according to:

$$P_{H,t} = ((1 - \xi_H)(\tilde{P}_{H,t})^{1-\theta} + \xi_H \left(\left(\frac{P_{H,t-1}}{P_{H,t-2}} \right)^{\chi_H} \pi_H^{1-\chi_H} P_{H,t-1} \right)^{1-\theta})^{\frac{1}{1-\theta}} \quad (9)$$

The same equation holds for the aggregate index of the price contracts $P_{X,t}$ set for the differentiated sold abroad product. As it is mentioned previously for the three types of final good firms, to produce the non-tradable final private consumption good Q_t^C , the firms purchases the domestic and foreign imported intermediate goods respectively H_t^C and IM_t^C using a constant-returns-to-scale CES technology:

$$Q_t^C = \left((v_C \mu_C + (1 - H_t^C))^{\frac{1}{\mu_C}} + (1 - v_C)^{\frac{1}{\mu_C}} (1 - \Gamma_{IM^C}) \left(\frac{IM_t^C}{Q_t^C} \right) \right)^{-\frac{1}{\mu_C}} IM_t^C \quad (10)$$

Where $\Gamma_{IM^C} \left(\frac{IM_t^C}{Q_t^C} \right)$ is the import adjustment cost faced by the consumption-good firms when adjusting the use of imports i.e. its imported share of inputs in the production of the final consumption good. This cost is linked to the import adjustment cost of the consumption parameter γ_{IM^C} . $\mu_C > 1$ is the intratemporal elasticity of substitution between the bundles of domestic and foreign intermediate goods. v_C defines the home bias in the production of the final good's consumption toward domestic intermediate goods. The weight of the inputs in the consumption basket are defined as $(1 - v_C)$ and v_C . It is worth stating that $H_{f,t}^C$ and $IM_{f^*,t}^C$ are respectively the use of the intermediate goods produced by the domestic and the foreign firm or foreign exporter f and f^* . $\theta^* > 1$ are the intratemporal elasticities of substitution between the domestic and foreign intermediate goods. After choosing the optimal use of each intermediate good f and f^* by the consumption good firms, the latter will combine the domestic and foreign intermediate good bundles H_t^C and IM_t^C that minimize the total input cost $P_{H,t} H_t^C + P_{IM,t} IM_t^C$ subject to aggregation constraint Q_t^C mentioned above so that the unit price of the private consumption $P_{C,t}$ and the demand functions for the intermediate good H_t^C and IM_t^C are obtained respectively. The same reasoning holds for the modeling of the non tradable final private investment good Q_t^I . The firms combines its purchase of the domestically-produced intermediate goods and the imported foreign intermediate goods respectively H_t^I and IM_t^I , using a constant-returns-to-scale CES technology. Then, the final non tradable public consumption good Q_t^G is assumed to be only made of domestic intermediate good; that is $Q_t^G = H_t^G$. The optimal demand

for the domestic intermediate good f $H_{f,t}^G$ is linked on the unit price of the public consumption good $P_{G,t} = P_{H,t}$. The demand for the domestic and foreign intermediate goods f and f^* are obtained through aggregating across the three final-good firms where: $H_t = H_t^C + H_t^I + H_t^G$ and $IM_t = IM_t^C + IM_t^I$. When it comes to the fiscal authority, the CMS assumption is considered. In this case, the fiscal domestic and foreign authority purchases units of the public consumption good G_t with price $P_{G,t}$, distribute transfer TR_t to each household group in unequal amounts, issue bonds to refinance its debt B_t , earns seignorage on outstanding money holdings, M_{t-1} , levies taxes on consumption, labor, capital and dividends and adjusts expenditures and budget financing accordingly (See the period-by-period budget constraint of the fiscal authority above). On the expenditure side, two alternative instruments are considered: the real transfer, the real government consumption and the lump sum taxes. Beginning with the government consumption consolidation strategy, the fiscal authority adjusts the consumption spending as a share of steady-state nominal output, $g_t = P_{G,t} G_t / P_Y Y$. This final public consumption good, follows the autoregressive process. Thus ρ_g is the autoregressive coefficient of government consumption and $\varepsilon_{g,t}$ is a white noise shock to government expenditure. Turning to the transfer, the fiscal policy adjust the transfer as a fraction of the steady-state nominal output $t_{tr} = TR_t / P_Y Y$. It is assumed like Coenen et al. (2007) that the fiscal policy via transfers is unevenly distributed across the two types of household, favoring the households J over the household I. Like (Coenen et al. 2008), it is assumed that the loss in revenue is financed by a decrease in the fiscal authority's transfer payments to households such that the government spending and debt-to-output ratios remain unchanged in the long run. The transfer evolves according to the autoregressive process. This is explained by the autoregressive coefficient of the public transfers ρ_{tr} . In fact the steady state value of government transfers is defined by t^r and the white noise shock to government transfers by ε_{tr} . These expenditures are financed by a different types of distortionary taxes, including taxes on consumption spending, labor and capital income. The other distortionary taxes are exogenously set by the fiscal authority considered as constant $\tau_t^X = \tau^X$ with $X = C, D, K, N, W_h$ and W_f . To model the Tunisian monetary authority, we refer to the outcome of Ben Chalbia (2010) who displayed that the Central Bank of Tunisia is directed more towards the future, precisely a typical Taylor interest rate rule under the forward-looking version featuring the interest-rate smoothing.

$$R_t^A = \varphi_R R_{t-1}^A + (1 - \varphi_R) [R^A + \varphi_\pi \left(\frac{P_{C,t}}{P_{C,t-4}} - \pi \right) + \varphi_{sy} \left(\frac{Y_t}{Y_{t-1}} - g_y \right) + \varphi_s (S_t - S_{t-1}) + \varepsilon_{R,t}] \quad (11)$$

This equation is determined in terms of the consumer price inflation and a quarterly output growth to provide an additional information on the future path of the inflation and the output. Also it is crucial to mention that the Taylor equation is enriched with the exchange rate as the Tunisian monetary authority is assumed to follow a flexible exchange rate regime. Where π is the annual inflation target of the monetary authority, $R^4 = \beta^{-4}\pi$ is the annualized quarterly nominal equilibrium interest rate, g_y is the rate of the output growth in the steady state (assumed to equal 1). The term $\varepsilon_{R,t}$ is the white noise shock to the interest rule or the monetary policy shock. It is worth to remember that the foreign economy, follows the CMS representation. Also the same formulation are considered for the market clearing conditions holding in the equilibrium, except some modifications in the labor market. These modifications concern the degree of the wage dispersion indices stated in a recursive formulation which are defined as follows:

$$s_{I,t} = (1 - \xi_I) \left(\frac{\tilde{W}_{I,t}}{W_{I,t}} \right)^{-\eta_I} + \xi_I \left(\pi_{c,t-1}^{\chi_I} \frac{\pi_C^{1-\chi_I}}{\pi_{W_{I,t}}} \right)^{-\eta_I} s_{I,t-1} \tag{12}$$

$$s_{J,t} = (1 - \xi_J) \left(\frac{\tilde{W}_{J,t}}{P_Y Y_t} \right) \left(\frac{W_{J,t}}{P_Y Y_t} \right)^{-1})^{-\eta_J} + \xi_J \left(\pi_{c,t-1}^{\chi_J} \frac{\pi_C^{1-\chi_J}}{\pi_{W_{J,t}}} \right)^{-\eta_J} s_{J,t-1} \tag{13}$$

Where $\pi_{W_{I,t}}$ and $\pi_{W_{J,t}}$ are the wage inflation rates of the household I and J. The aggregate demand for the labour services of variety i and j across the intermediate-good firms are respectively N_t^I and N_t^J . The same process is considered for the differentiated labor services supplied by household J.

CALIBRATION AND SIMULATIONS

Calibration

There are different methods to estimate and evaluate DSGE models. In this case, the model is not estimated but instead calibrated on the Tunisian economy using an annual data over 1980–2011. Table 1 and 2 summarize the main differences between the block of the two regions.

Table 1: Macroeconomic Aggregates (steady state ratios)

Ratio	Euro Area	Tunisia
$P_C C / P_Y Y$	0.60	0.63
$P_I I / P_Y Y$	0.22	0.11
$P_G G / P_Y Y$	0.18	0.16
$P_{IM} IM / P_Y Y$	0.18	0.46
$M / (1 + \tau_c) P_C C$	1.34	0.21
$P_{IM} IM^c / P_Y Y$	0.05	0.13
$P_{IM} IM^I / P_Y Y$	0.13	0.09
$B / P_Y Y$	2.4	2.30
$D / P_Y Y$	0	0

The table shows the steady state ratios of the main expenditure categories over nominal output. In order to obtain an accurate result, we try to fit the NAWM to the stylized facts of the Tunisian economy data which is not an easy task for a model adapted to the Euro area. The calibration for the Euro Area is similar to the one of (Coenen et al, 2008). However for Tunisia, we follow the traditional literature and the microeconomic evidence. In fact the national accounts are considered from 1980 to 2011 to set the steady-state ratios in the home country. The latter is provided by the International Financial Statistics (IFS) and the World Bank data. However concerning Tunisia, the parameter's value are taken similar to the one of emerging market in the absence of reasonable proxies in the literature. This model involves 138 parameters comprised of aggregate share or ratios, steady state values, 231 endogenous variables and 21 shocks. The table 1 corresponds to the macroeconomic aggregates or the steady state ratios (see the annex1 for more details). The shares of the aggregate demand components in GDP ($P_C C / P_Y Y, P_I I / P_Y Y, P_G G / P_Y Y$) are based on the sample average calculated from the national accounts. Beginning with the ratio of the private consumption to output $P_C C / P_Y Y$, it is set to 0.63 in Tunisia. This value is not far from the one in Turkey which is calibrated to 0.7 by Çebi (2012). To obtain a consistent specification of the steady state trade linkage, it is elementary to calibrate the import to output ratio $P_{IM} IM / P_Y Y$ or the degree of openness, which is 0.4633; the share of import in private consumption good $P_{IM} IM^c / P_Y Y$ that is 0.13 and the share of private investment good $P_{IM} IM^I / P_Y Y$ which is 0.09 in Tunisia. The money to consumption ratio $M / (1 + \tau_c) P_C C$ is 0.21. Moreover, to measure a country's ability to make future payments on its debt, it is crucial to deal with the steady state of the government debt to GDP ratio $B / P_Y Y$. The steady state ratios of government debt to output ratio is fixed to 2.3. For its part, the share of government consumption to output $P_G G / P_Y Y$, is calibrated to its real value 0.16, on the basis of the annually IFS Tunisian data.

Table 2: Calibrated Parameters and Steady State Variables (Household)

Household	Euro Area	Tunisia
s	0.98	0.01 (relative to Africa)
σ	2.00	1.00
β	0.99	0.98
κ	0.60	0.50
ζ	2.00	2.00
δ	0.02	0.02
ω	0.25	0.53
ξ_I, ξ_J	0.75	0.75
χ_I, χ_J	0.75	0.75

The dividend income-to-output ratio $D/P_Y Y$ is assumed to be zero in the steady state. Then, the share of private investment to output $P_I I/P_Y Y$ is set to 0.11. The calibrated parameters and the steady state variables concerning the household's behavior is exhibited in the table 2 (see the annex 1 for more details). In fact, the financial market frictions w related to the size of the household J is close to 53 %. The rate of time preference or the subjective discount rate β is equal to 0.98. The annual depreciation rate of the private and public capital δ amounts to 0.025 across all regions. This value is detected by Ben Aissa and Rebei (2012) and Jouini and Rebei (2014) in Tunisia. It is standard in the literature (see Cooley and Prescott, 1995) or (Burda and Weder, 2002). The production share of capital income in GDP, $\alpha=0.3$ is opted for Tunisia which is very close to a typical assumption found in the literature usually around 1/3. Hence the estimate seems very reasonable. However, there is no agreement in choosing the magnitude of the inverse intertemporal elasticity of substitution σ . Generally the estimates are ranging from 1 to 4 in the literature (Lehmus, 2011). In Tunisia it amounts to 1 as the value chosen by Ben Aissa and Rebei (2012), Gouvea et al. (2008); Valli and De Carvalho (2010) in Brazil. The inverse labor supply Frisch elasticity ζ is picked to 2. The range commonly adopted in the business cycle literature is between 1 and 2 especially in the emerging market as detected by Jacquinot and Straub (2008) as well as Gouvea et al. (2008) in Brazil. Our calibration of the degree of habit formation κ is fixed to 0.5, in line with the research carried out by Ben Aissa and Rebei (2012) in the Tunisian economy following the changes in the level of consumption in developing countries. The calibration of the Calvo parameter determining the persistence of wage setting ξ_I, ξ_J , or the fraction of both household members I and J not setting wages optimally each quarter corresponds to 0.75, consistently with Ben aissa and Rebei (2012) and Jacquinot and Straub (2008). The degree of wage indexation χ_I, χ_J is also selected to 0.75. Turning to the analysis of the table 3 relative to the intermediate good firms. First, the share of the fixed cost in the production Ψ is taken so that to ensure zero profits in the steady state, and discourage the other firms to enter the market in the long run, as documented by Valli and De Carvalho, (2010); Coenen et al. (2007); Christoffel et al. (2008). The value is picked to 0.143, similar to that employed in Emerging Asia (see Jacquinot and Straub, 2008). Second, the steady state productivity level z is normalized to unity (stationary). Third, the calvo probability of the intermediate –good firm's fraction selling their differentiated outputs in the domestic markets ξ_H or the fraction of home firms not setting their prices optimally each quarter corresponds to 0.75. The latter is consistent with Medina and Soto (2007) respectively in Columbia and in Chile. For its parts, the degree of indexation χ_H is set to 0.5 (see Valli and de Carvelho, 2010).

The fraction of foreign firms not setting foreign prices optimally ξ_x is fixed to 0.3 and the corresponding degree of price indexation χ_x is fixed to 0.5. The intratemporal elasticity of substitution η_I and η_J between the household-specific bundles for the differentiated labor services, are designed to 6. This value is also noticed in Brazil by De Carvalho and Valli (2011). On the other side the information related to the final good firms are reported in the table 4 (see the annex 1 for more details). The intratemporal price elasticities of substitution between the home and foreign intermediate goods in forming the consumption and investment bundles μ_C, μ_I is selected to 1.5. This value is approximate to the one set by Çebi (2012) in Turkey. The home bias parameter, in particular the one that corresponds to the share of domestically-produced goods in the total private consumption expenditure v_c , is selected such that it equals its empirical counterpart, precisely as 0.49 in Tunisia. This value is not very far from the one opted in Chile 0.65 by Medina and Soto (2007).

Table 3: Intermediate good firms

Intermediate good firms	Euro area	Tunisia
α	0.30	0.30
Ψ	0.20	0.14
z	1.00	1.00
ρ_z	0.90	0.80
η	6.00	6.00
$\eta_I \eta_J$	6.00	6.00
ξ_H	0.90	0.75
ξ_x	0.30	0.30
χ_H	0.50	0.50
χ_x	0.50	0.50

Note: The subscript I represent the unconstrained households while J represent the liquidity constrained household in the model. The same thing for H which stands for the tradable sector while X represents the export sector in the model

Meanwhile the home bias in the production of investment final goods v_I is calculated to 0.5 in Tunisia see Medina and Soto (2007) and Burriel et al. (2010) in the Chilean economy and the Spanish economy. De Carvalho and Valli (2011) calibrate the home biases v_c and v_I from the demand equations of imported goods using the steady state value for the supply of consumption and investment goods, and the import quantum. On the other hand, (Christoffel et al. 2008) chose steady-state values for the home-bias parameters v_c and v_I that allow the model to replicate the import content of consumption and investment spending—roughly 10 and 6

percent, expressed as shares of nominal GDP. Moreover, to ensure that the households' groups I and J work the same amount of hours, the labor demand bias v_w is calibrated to 0.05. Finally, the intratemporal elasticity of substitution designed as the price elasticity of demand between the domestic and foreign intermediate goods for a specific intermediate-good variety θ is picked to 6, implying a steady-state mark-up of 20%. A common value used in the literature, is confirmed by De Carvalho and Valli (2011) and Galí et al. (2005) for a small open economy in all. The calibration is still pursued with the monetary authority policy that is observed in the table 5. For the parameter related to the interest-rate response coefficients on the annual inflation in term of deviation from an inflation target, also called the interest rate sensitivity to inflation gap ϕ_π , our reference is Çebi (2012), who took a mean of 1.5 in Turkey, and Jouini and Rebei (2014) in Tunisia. Also, based on the calibration of this latter and on Gouvea et al. (2008), the interest rate sensitivity to the output growth gap ϕ_{s_y} corresponds to 0.25 in Tunisia. The coefficient on the lagged interest rate or the degree of the interest rate inertia ϕ_R , is designated to 0.5 with reference to the prior mean for the interest rate smoothing parameter chosen by Jouini and Rebei (2014) and Çebi et al. (2012). On the other side, the response of monetary authority to exchange rate variation ϕ_s is set to 0.8. The steady state of inflation π is selected to 1. In the emergent economies like Brazil, this value amounts to 1.04 (see Valli and De Carvalho (2010)). After calibrating the monetary authority policy's parameters we now perform the fiscal authority's parameters observed in the table 6 (see the annex 1). First, the sensitivity of the aggregate lump-sum taxes with respect to the government debt-to-output ratio ϕ_{BY} is designated to 0.046 in Tunisia which is close to the value proposed by De Carvalho and Valli (2011) and Gouvea et al. (2008) in Brazil. Second, the Government debt-to-output ratio B^y is set to 2.32. Third, the government transfers-to-output ratio or the government transfer (tr) is picked so that the fiscal authority's budget constraint is balanced at the neutral debt-to-output ratio or satisfied in the long run, is set to 0.05 in Tunisia. This ratio is higher in the Euro Area due to a more generous unemployment benefit system, a higher emphasis on pension schemes (Roeger and in't Veld, 2009). The other parameter which concerns the government consumption-to-output ratio (g) or the government expenditure, is based on the national accounts dataset selected as 0.16. Both the government spending-to-output ratio ρ_g or the persistence of public consumption and the public transfer-to-output ratio ρ_{tr} , have an autoregressive coefficient of 0.90. Moving to the tax rates calibration, some values are calculated based on the current tax law of Tunisia on average (see table 6 annex 1). They are presented as follow: 26.83% for the tax on income profits and capital; $\tau^c = 29.5\%$ for the consumption taxes, $\tau^{wh} = 7.64\%$ and $\tau^{wf} = 17.21\%$ for

subsequently the social contribution of the employees and employers, 0 for the tax rate on dividend τ_D , as the dividend versed by the Tunisian societies are not submitted to tax and $\tau^N = 0.2$ for the labor income tax rate. Eventually, table 7 summarize the adjustment and transaction cost. In fact γ_{v2} appearing in the functional form of the consumption transaction for the domestic economy, is opted consistently to Coenen et al. (2008) and Jacquinet and Straub (2008) equal to 0.150.

Table 4: Final good firms

Final good firms	Euro area	Tunisia
v_C	0.92	0.49
v_I	0.41	0.50
v_w	1.00	0.05
μ_C	1.50	1.50
μ_I	1.50	1.50
θ	6.00	6.00

Note: The subscript C represents consumption goods sector while I stands for the investment goods sector. IM means the imported goods sector

For the other parameter γ_{v1} , we refer to Jacquinet and Straub(2008) in emerging Asia and set it to 0.029 in Tunisia. In addition, the investment adjustment cost function (the share of domestic good in the investment) γ_I is calibrated to 4.58 in Tunisia based on IFS. In fact, based on the value of a prior distribution set on Brazil to 4 by Gouvea et al. (2008) or 3 set by Valli and De Carvalho (2010). The capital adjustment cost parameter value γ_{u1} is set to 0.05 following Valli and De Carvalho (2010). In addition to γ_{u2} that is picked to 0.007 with reference to Jacquinet and Straub (2008); Valli and De Carvalho (2010, 2011). For the parameters controlling the adjustment cost related to changing the import share in consumption γ_{im^c} , they are detected to 4 in Tunisia based on the value set in Brazil, to dampen the sensitivity of consumption to the change of the terms of trade.

Table 5: Monetary authority

Monetary authority	Euro Area	Tunisia
Π	1.02	1.00
ϕ_{gy}	0.10	0.25
ϕ_R	0.95	0.50
ϕ_π	2.00	1.50
ϕ_s	-	0.80

This parameter determines the ability of household I to borrow from abroad in the short to medium run. It influences the profile of its intertemporal consumption and investment decision. Besides, the parameters of the import adjustment cost of investment γ_{IM^I} , takes the value of 2.5 (see Jacquinot and Straub, 2008). To end, the parameter governing the intermediation cost function, also called the risk premium γ_{BF} , is around 0.05 in Tunisia (see Jacquinot and Straub, 2008) so that the evolution of net foreign assets has a small impact on the exchange rate and the trade in the short run. It enables the net foreign asset position to be stabilized to zero in the long run.

Table 6: Fiscal policy

Fiscal authority	Euro Area	Tunisia
B^Y	2.4	2.32
ϕ_{By}	0.10	0.04
g	0.18	0.16
ρ_g	0.90	0.90
ρ_{tr}	0.90	0.90
tr	0.19	0.05
τ^c	0.18	0.29
τ^D	0.00	0.00
τ^N	0.12	0.20
τ^{Wh}	0.11	0.07
τ^{Wf}	0.21	0.17

Note: The calibration of the tax rates of the Euro Area, are similar to the one selected by Christoffel et al.(2008) who provide the information from the OECD (2004) and Eurostat (2006).

Simulation and Policy analysis

The simulation in this paper concerns the dynamic responses effects of monetary and fiscal shocks like the government spending and the transfer to household shock as well as the dynamic properties of the NAWM illustrated in the figure 1. This figure depicts the dynamic responses of the domestic variables to a monetary policy tightening represented by a black line, equal to a 1% increase in the annualized nominal interest rate; to a persistent government spending shock, represented by a blue line, equal to a 1% increase in the steady- state output and to a persistent transfer shock, represented by a green dashed line, equal to 1% increase in the steady-state output. It is crucial to note that all the dynamic responses are reported as percentage deviations from the steady state. Also, all the simulations were achieved using the function “stoch_simul” of DYNARE at MATLAB.

Table 7: Adjustment and transaction cost

Adjustment and transaction costs	Euro Area	Tunisia
γ_{v1}	0.28	0.02
γ_{v2}	0.15	0.15
γ_{u1}	0.03	0.05
γ_{u2}	0	0
γ_I	3	4.58
γ_{IM^C}	2.5	4
γ_{IM^I}	0	5
γ_{BF}	0.01	0.05

The expenditure based consolidation

After the calibration, we describe the dynamic response of the macroeconomic variables following the monetary, government expenditure and the transfer shock.

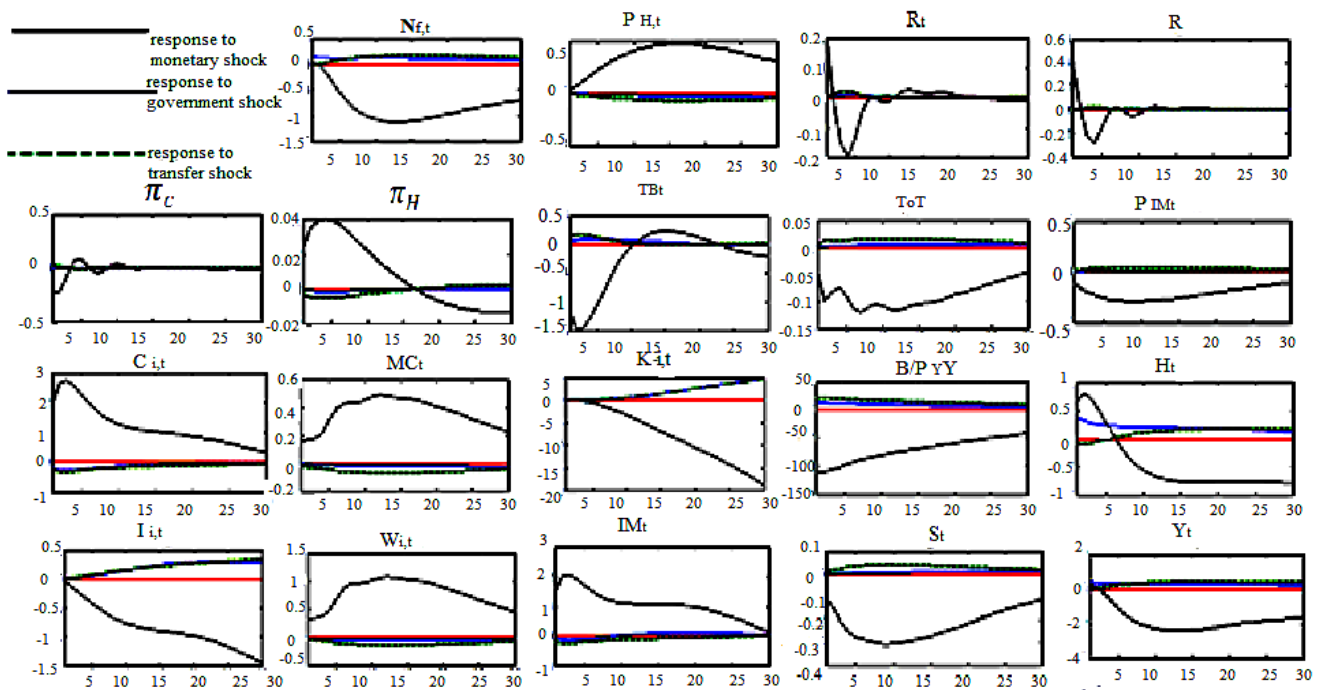
Monetary shock

After a positive interest rate there is a fall in the output Y_t as emphasized by Çebi (2012); Ratto et al. (2009); Christoffel et al. (2008); Fabia et Valli (2011); Burriel et al. (2010). This decline will put pressure on the consumption and investment and the labor demand $N_{f,t}$. Indeed Christoffel et al. (2008) elucidated the drop of the investment by a temporally reduction in the domestic demand. It is crucial to remember the link between the capital $K_{i,t}$, the interest rate and the debt to output ratio. Following this shock, it is noticed that the interest rate declines then moves to zero which will boost the debt to output ratio. De Castro et al. (2011) thought that keeping the interest rate fixed for a certain period yields a fall in the inflation. On the other hand, there is a lower demand for the capital. For its parts, the inflation especially the consumer's price inflation π_c , slightly pushes up then levels off.

Christoffel et al. (2008) explicated this decline by a fall in the domestic prices. The next variable is the terms of trade ToT which is defined by the domestic import price relative to the export price in domestic currency. Following the monetary shock, it falls then will recover. Indeed, Christoffel et al. (2008) and Coenen et al. (2008) claimed that the improved ToT lead to changes from domestic towards imported goods. More precisely, Coenen et al. (2008) justified this improvement by the appreciation of the domestic currency. When it comes to the real wages $W_{i,t}$, it is noticed an upward trend in the first 10 quarters that will depreciates in the medium run. Indeed, De Castro et al. (2011) and Fabia et al. (2011) elucidated the delayed reduction in the wage by the curtailed demand for the labor by the firms, due to the decline in

the output. This fall put downward pressure on the domestic price π_H . As far as the import IM_t is concerned, there is a continued fall of the latter. In this sense De Castro et al. (2011) pointed out that this fall is caused by the decline in the output. Likewise, the import prices $P_{IM,t}$ dips. Finally, we explain the relationship between the trade balance TB_t , the real exchange rate and the export. As shown in figure 1, there is a negative impact on the export. That is why the trade balance stabilizes in the long run. Indeed Christoffel et al. (2008) and De Castro et al. (2011) interpreted the reduction in the exports, by the improvement of the ToT inducing a switching effect to the imported goods. The real exchange rate, follows nearly the same trends of the ToT .

Figure 1: Dynamic responses to a monetary, government and transfer shock



Transfer shock

As regards the output, the latter hikes in short run, pushing up the consumption $C_{i,t}$ and the investment $I_{i,t}$, then will drop in the long run. Precisely, the consumption decelerates by a small amount at the beginning of the period then will sharply recognize an ascension in the medium and the long run. In fact, likewise many authors Ratto et al. (2009); Fabia and Valli, (2011); Forni et al. (2009), it is found that the rise in the consumption will put upward pressure on the wage in the long run. Moreover as mentioned before, the investment hikes. In this field, Coenen et al. (2008) revealed that the unconstrained household ameliorates the investment purchases. As they anticipate a rise in the opportunity cost of capital formation, encouraged by the decline

in the interest rate R_t . For its parts, the interest rate delicately pushes up then levels off promoting the accumulation of the capital. That is why the debt falls. In addition the wages declines in the medium run then will pushes up for both household. Another pictures emerges with the ToT , it rises in the first 10 quarters then will decline in the long run. Finally, we note a decrease in the trade balance as well as the import.

Government shock

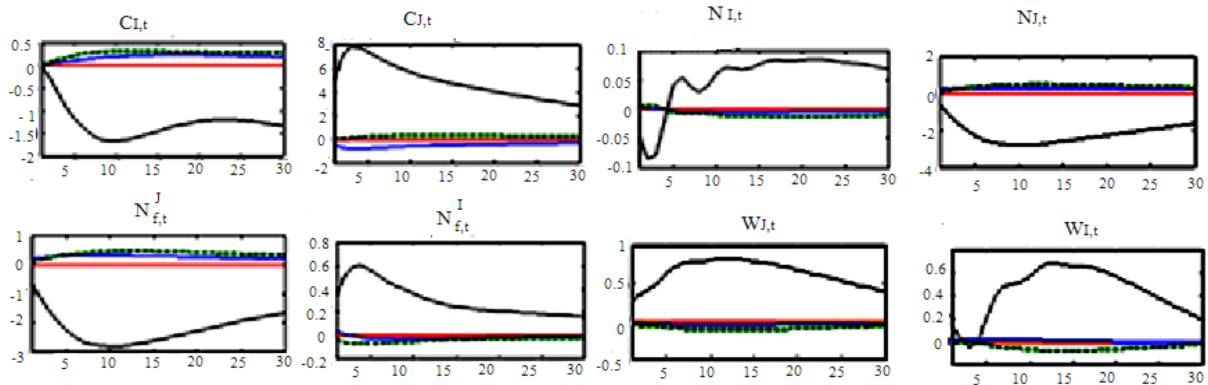
When it comes to the government shock, one can see that the decline of the output is moderate. This is explained by the decrease in the labor supply pushing down the export of the economy. Also the consumption slightly goes down, then will sharply boost in the long run. This is induced by the rise of the employment. At the same time the investment is moving up because of the decline in the interest rate. According to Papageorgiou (2012) and Coenen et al. (2008), the positive impact of the investment is due to the expansion in hours worked that will enhance the marginal product of capital. On the other hand, the interest rate R_t goes up just for a short moment, putting downward pressure on the debt. Then will fall in the medium and the long run putting upward pressure on the investment and the consumption. Due to this positive impact on the investment and the increase in hours worked, the capital rises, as discussed by Papageorgiou (2012) and Coenen et al. (2008). Conversely, the inflation has a downward trend, because of the depreciation in the marginal cost of the consumption goods. Concerning the wages, there is an initial decline which will sharply hikes in the long run. Moreover, there is a small decline in the import at the beginning of the period, then will peaks sharply in the medium and the long run. We also note an improvement of the ToT (decrease), which is interpreted by the increase in the imports. In fact, the (TOT) deteriorates the trade balance. This trend can be clarified by the increase in the import in the long run, even if there is a small development in the exchange rate.

The distributional effect

The figure 2 depicts the distributional effects of a gradually permanent increase in the monetary interest rate (represented by a black solid line), the government spending shock (represented by a blue solid line) and the transfer to household shock (represented by a green dashed line), equal to 1% increase in steady-state output, on the domestic variables. The dynamic effects are reported as percentage deviations from the initial steady state. Starting with the government consumption shock, the liquidity constrained households J cut back moderately their consumption $C_{J,t}$ due to the marginal drop in their wage, then will be recovered in the medium

term as their wage hikes Unlike the consumption $C_{I,t}$ of the household I which is in expansion. In this field, Coenen et al. (2008) added that the rise in government consumption absorbs part of the economy's resources yielding a negative wealth impact especially on the part of the household J. As they feel poorer, they will diminish their consumption and improve their labour supply $N_{J,t}$. Following the strategy of increasing the transfer, the household J still reduce their consumption purchase marginally, then will strongly enhance it. Yet again, Coenen et al. (2008) pointed out that there is a loss of income because of the unequal financing requirement that they face.

Figure 2: Distributional effects of permanent increase in a monetary interest rate shock, government spending and transfer shock to household



The Revenue based consolidation

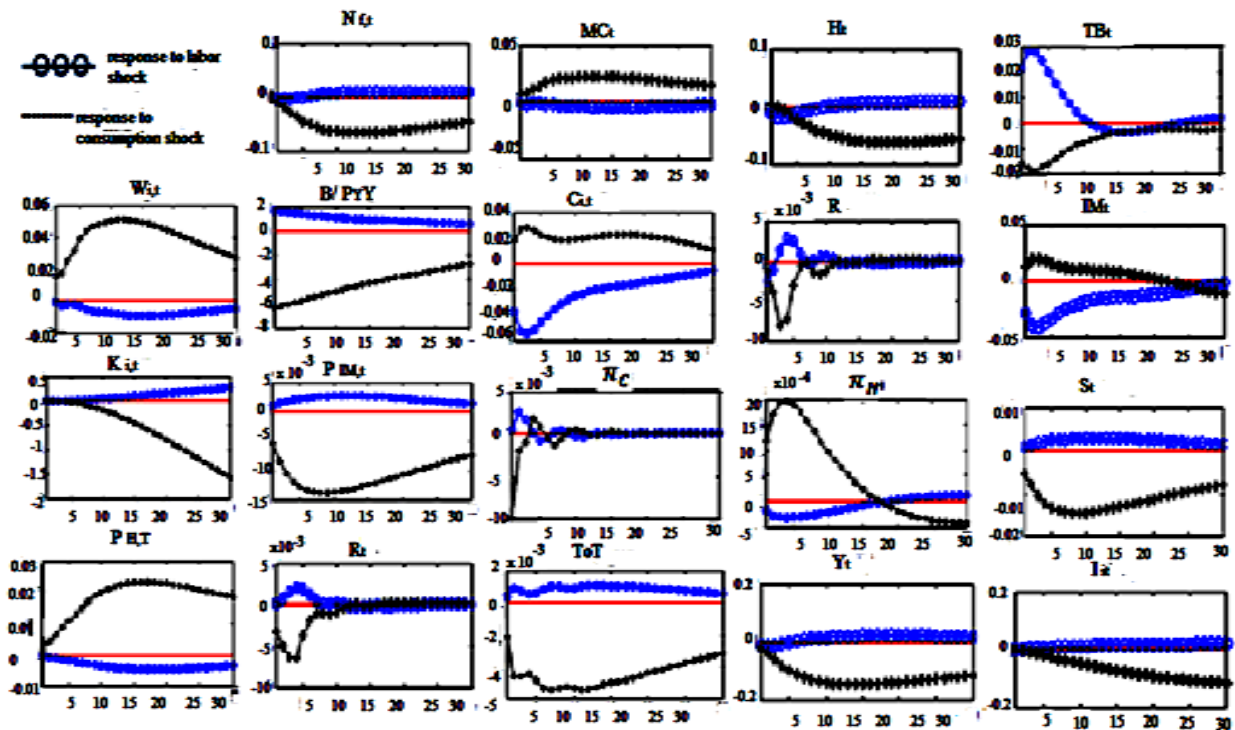
Concerning the dynamic effect on the revenue- based consolidation, the figure 3 summarizes the impact of a permanent reduction in the consumption and the labor income taxes.

Labor shock

Starting by the labor shock, the latter pushes the output Y_t up. In this perspective, Papageorgiou (2012) who evaluated the permanent reduction in the labor income tax accompanied by a permanent increase in the consumption taxes, claimed that the most effective policy to boost the output, promote the welfare and stimulate the economy is to reduce the labor income taxes. He also highlighted that this strategy implies a rise in the labor supply of the household as well as the consumption and the hours worked. Similarly Forni et al. (2009) interpreted the rise in the output by the increase in the aggregate demand. In addition to Kitao (2010) who justified the higher output and the rapid economic growth by a positive response of both investment and consumption. Moving to the effect on the consumption variable, the latter initially dampens then

will boost sharply in the medium and the long run. When it comes to the real wages, $W_{i,t}$ the latter dampens in the short to medium run but rises in the long run. In this context, Stähler and Thomas (2011) clarified the depression of the wages by the importance of the unemployment. This latter is generated by the drop of the output. On the other hand, the middle left panel of the Figure 3, shows that the labor income taxes induces an ascension of the capital $K_{i,t}$. In this context Papageorgiou (2012) added that the increases in hours worked has a positive impact on the marginal product of the private capital. The latter encourages the rise of the future capital formation which in return enhances the output in the long run. In the same way Kitao (2010) detected a rise in capital when cutting the temporary income tax. Then, consistently with Stähler and Thomas (2011), there is a development in the investment $I_{i,t}$ due the fall in the interest rate. In fact this fall is detected in the medium and the long run then will levels. The (ToT) slightly goes up in the first ten quarters then will decline. Nevertheless, the import initially cuts down which will then sharply jumps in the long and the medium run. Finally regarding the debt to output, we found that the labor income taxes drives down this debt in the short to medium run. In this perspective, Papageorgiou (2012) précised that the reduction in labor taxes financed by higher consumption taxes not only stimulates the economy but also reduces the debt to output ratio.

Figure 3: Dynamic Responses to a consumption and labor shock

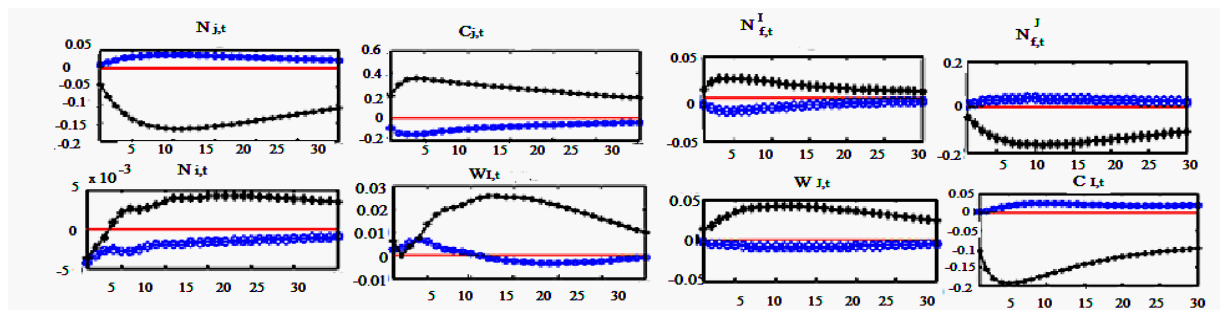


Consumption shock

When it comes to the consumption shock, the output sharply declines in the first 10 quarters, then will delicately rises. Besides the consumption initially rises then slightly dampens in the medium and the long run. Furthermore, the real wages initially pushes up then will decline in the medium and the long run. Turning to the (ToT) , its movement shifts across the time. It declines then will moderately rises. There is a fall in the capital as well as the investment. Indeed Forni et al. (2009) clarified that the smoother increase in the Ricardian consumption gradually shifts resources away from the investment. So when there is an income increases, the household I does not rely on the economy's capital stock. To end, we should not forget to describe the effect on the trade balance TB_t , the import IM_t and the exchange rate S_t variables. In fact, there is still a reduction in the import yielding an improvement of the trade balance. The latter declines marginally then will picks and stabilize in the long run. Furthermore, the exchange rate goes down. This fall is due to the decline in the export that will in return enhance the debt. Moreover, with the labor income and consumption taxes shocks, the consumer price index π_c slightly pushes up in the short run then will stabilize in the medium and the long run. This is also observed by Forni et al.(2009) and Stähler and Thomas (2011). In fact Çebi (2012) elucidated the initial rise of the inflation by the amelioration of the marginal cost. However, the decline in the inflation puts downward pressure on the interest rate (Forni et al. 2009).

The distributional effect

Figure 4: Distributional effect of consumption and labor income tax shock



In an attempt to highlight the influences of the propagation of consumption and labor income shocks on the two types of households 's behavior, the figure 4 compares the dynamic responses of many selected variables. It is observed that the consumption tax shock ameliorates the consumption $C_{J,t}$ of the constrained household J when their wage $W_{J,t}$ is improved, then will reduce it as their wage drops. The amelioration of the household J's wages

is associated with a slowdown of their labor supply $N_{j,t}$. To smooth their consumption, they should build up their labor supply. However the consumption of the unconstrained household I, $C_{i,t}$ dampen only in the short run, then will recover in the long run. Their wage that witnesses a little fall will recognize an ascension. In contradiction, it will depreciates in the medium run. The ensuing drop of the wages followed by a permanent reduction in the consumption taxes explained the depreciation of the non constrained household's consumption $C_{i,t}$. Another cases appears with the labor income taxes shock, the distributional effect's figure illustrates that this shock encourages the work effort and the labor supply $N_{i,t}$ to hike, as well as the increase in hours worked mainly for the constrained household. This is because of the decline in their wages and in their consumption in the short run. The responses of the real wages seems also to follow the one found by Roeger and in't veld (2009) especially for the constrained household. However, there is an improvement in the consumption of the non constrained household as their wages rises in the short run, then will drive down.

LONG RUN EFFECTS OF THE TAX REFORM

The table 3 (for more details see the annex1) examines the long-run effects of reducing the level of the tax wedges to levels prevailing on the domestic and foreign variables. In this context, four alternative scenarios are exhibited. The transitional dynamics implied by such reductions is considered. Initiating with the revenue-based-consolidation strategies, the first panel of this table reports the long-run impact of unexpectedly reducing the consumption tax by 11.2%. This instrument affects the decisions of the households along the same consumption – leisure margin and allows them to increase their supply of labor services. In this context Coenen et al. (2008) ensured that the reduction in the consumption tax enhances the labor supply of the economy. However they reported that this technique encourages the purchasing power of the household's wage income. While the result displays that the real wage income of the household $W_{i,t}$ in this case is curtailed by -3.22%. This reduction is also found by Henry et al. (2008). It is observed that the reduction in the consumption tax-rates enables the development of the consumption $C_{i,t}$ by 5.9%. Concerning the capital accumulation $K_{i,t}$, it builds up by 83%. In this perspective, Coenen et al. (2008) highlighted this behavior by the positive effect of the increase in the hours worked. In return, the investment $I_{i,t}$ is delicately improved by 2.09%. As Burriel et al. (2010) and Coenen et al. (2007), we found that an unexpected reduction in the Value Added Taxes (VAT) has a long-run positive effect on the Tunisian economy as the output of the domestic economy Y_t hikes by 12.6%. This is explained by the increase in hours worked as well as the capital stock.

Table 8: Long run effects consolidation in Tunisia and The Euro Area in%

	Revenue consolidation strategy			overall tax wedge	Expenditure consolidation strategy	
Tunisia	$\Delta\tau^c = -0.112$	$\Delta\tau_{wN} = -0.068$	$\Delta\tau_{wH} = -0.04$	-0.221	$\Delta g = 0.0179$	$\Delta tr = 0.0179$
Y	12.60	5.79	4.14	22.59	0.46	-0.09
$C_{i,t}$	5.90	2.75	1.97	10.33	-0.23	-0.04
$I_{i,t}$	2.09	0.96	0.68	3.75	0.12	-0.01
$B/P_Y Y$	293.47	25.79	18.07	345.24	6.40	4.60
$K_{i,t}$	83.97	38.47	27.52	150.30	4.92	-0.63
$N_{i,t}$	0.07	0.32	0.23	0.64	0.00	0.00
$N_{j,t}$	9.73	1.99	1.40	13.05	0.26	-0.12
$N_{f,t}$	5.44	2.49	1.78	9.74	0.16	-0.04
$W_{i,t}$	-3.22	-1.524	-1.09	-5.51	0.04	0.02
ToT	0.39	0.17	0.12	0.71	-0.00	0.00
IM_t	1.07	0.48	0.35	1.92	-0.01	0
H_t^I	5.76	2.67	1.91	10.17	0.55	-0.04
Euro Area						
Y	0.13	0.05	0.04	0.24	0.00	0
$C_{i,t}$	0.73	0.33	0.24	1.32	-0.01	0

Note: This table presents the steady state effect reported as percentage deviation from the initial steady state for selected domestic and foreign variables of permanent percentage-point reductions in Tunisian tax wedges to levels prevailing in the Euro Area and an increase in the government and a transfer by a 1% of a steady state output

The result shows a slight enhancement of the ToT by 0.39%. The other revenue based-consolidation strategy concerns the reduction in the labor income tax. In a different spirit to Kitao (2010), it is discovered that the labor supply will boost because the wages $W_{i,t}$ demanded by the workers depreciates in this case by -1.524%. In this context, Stähler and Thomas (2011) affirmed that the workers claim weaker gross wages because the reduction in taxation enhances their take-home pay. For its part, the investment $I_{i,t}$ is surging by 0.96% due to the high labor supply as interpreted by Kitao (2010). As a consequence, the economy recognizes a rapid economic growth and a higher output which is developed by 5.799%. As the income becomes higher, our finding displays an expansion in the consumption $C_{i,t}$ which softly peaks by 2.75%. Although the consumers I increase their consumption more than the household J. For its

parts, the debt B_t becomes higher. Indeed Kitao (2010) revealed that when the labor income tax rate is kept low, the government budget constraint is satisfied by adjusting the amount of outstanding government debt. This tax cut allows the household to exploit the temporarily high returns from renting additional capital and labor. In this case, the capital goes up by 38, 47%. Besides, the import IM_t which slightly hikes by 0,489% .While the exports rises by 2,672%. Moving to the expenditure consolidation strategy specifically the increase in the transfer. We note a slight negative long run effect on the output by -0.095%. Coenen et al. (2008) explicated that the ascension in transfer dampens the labour supply of the household $N_{i,t}$ for any given wage rate especially for the household J while pushes up their disposable income. In the same context, Kitao (2010) justified the shortfall in the labor supply by the income effect as the disposable income rises with higher transfer.

On the other side, the government debt is surging by 4.6% to finance the additional expenditures as explained by Kitao (2010). This rise in the debt crowds out the private capital $K_{i,t}$ by -0, 63%, and puts downward pressure on the output and consumption. This author clarified that the rise in the debt after the transfer policy will put downward pressure on the labor supply and the saving of the households. Turning to the investment, there is a reduction by - 0.015% as well as the capital. According to Coenen et al. (2008) this reduction is due to the downturn in the economy's capital stock and the reduction in the marginal product of capital. In turn, both the consumption $C_{i,t}$ and the import cuts downs respectively by -0.046% and - 0.008%. The reduced import will bring down the price of imports $P_{IM,t}$ by -0,0073% to restore the long-run equilibrium characterized by the balanced trade. As a consequence, the terms of trade ToT decelerates by -0.0029 % so that there is an improvement in the ToT . This trend is also showed by Coenen et al. (2008).

Finally, another scenario will appear if the fiscal authority enhances its government consumption expenditure. This strategy generates a negative wealth effect on the part of households as they cut back consumption purchases by -0.235% (see Coenen et al. 2008). On the other hand, the labor supply $N_{J,t}$ is developed especially for the household J, by 0.2696%. They also emphasized that the investment $I_{i,t}$ boosts (by 0.122 %), due to the positive impact of the hours worked on the marginal product of capital. Consequently, this positive impact on the capital and the investment strengthened the output Y_t by roughly 0.46%. Also, the exports H_t is ameliorated by 0.55%. Whereas it pushes down the imports IM_t by -0.015%. Nevertheless, a different behavior appears with the real wages $W_{i,t}$. It is ameliorated by a small amount of 0.048%. Finally, the ToT is slightly improved by -0.0054 %.

MEASURING THE MODEL FIT

For the calibrated model, Malley et al.(2009) suggested two methods to ensure that the model fits the data. For example, the method of Watson (1993) who emphasized on the covariance function ACF and compare the one of the model to the one of the data. Also the method of Christiano et al. (2005) who do the same exercise based on the impulse response function. Both measures need comparison of an estimated VAR with the calibrated VAR. Yet again Lees et al. (2011) reports the match of the model to the key selected moments in the data for the interest rate, inflation, growth rate of output, the change in exchange rate and the terms of trade through the mean, the standard deviation and the distribution of the first order autocorrelation statistics for the estimated model. However we simply compare the theoretical selected moments and implied by the model NAWM to the simulated moments given by the sample data. The table 9 report the mean and variance of the most important endogenous variables implied by the NAWM and the sample moments based on the observed data over the calibration period. Regarding the sample mean as well as the variances, we deduce from Table 9 that the NAWM model broadly fits the data. The variances and the mean of variables obtained from data and that of model are close to each other. The majority of the variables in the table have a data-based (sample) mean that is softly higher than the model-based mean. Similarly for the variance, the real GDP, consumption, investment, have a data-based sample volatility measure slightly greater that the NAWM model .

Table 9: Sample mean and variance

Variable	mean		Variance	
	simulated	theoretical	simulated	Theoretical
Real GDP	1.832	1.805	0.026	0.019
Consumption	3.14	3.110	0.049	0.038
Investment	0.70	0.599	0.098	0.089
The terms of trade	0.843	0.842	0	0
Nominal interest rate	1.007	1.007	0	0
Real effective exchange rate	0.800	0.797	0	0
Consumption deflator inflation	0.999	0.999	0	0
Debt to output	-8.492	-9.065	0	0

Note: For the simulated moments of the variables, the results are based on 2000 draws of the NAWM's structural parameters.

CONCLUSION

In this paper, we develop a calibrated two-country version of the NAWM and try to adapt it in the Tunisian economy. In fact some notions of the CMS model, previously mentioned, are revised and corrected so as to take into consideration the features of an emergent country. Also, we

propose a reform which demonstrate that both expenditure and revenue-based consolidation measures have an economically significant impact on the macroeconomic aggregates. Depending on the implemented consolidation scheme, it is discovered that the revenue-based consolidation policies when lowering distortionary taxes yields a positive long run effect on the output. In contrast, the expenditure-based policies which deteriorate the output in a long run. However it exhibits a moderate increase in the household wages as well as a slight rise in the consumption in a long run . Also this technique pushes up the investment in a short and a long run. Also, depending on the fiscal instrument used when measuring the impact of the tax reforms, the fiscal consolidation may have a pronounced distributional effects with the presence of heterogeneous households. In future researches many fiscal instruments can be analyzed. For example the techniques proposed by Stähler and Thomas (2011) related to the public investment cuts, the public purchases cuts, the reduction in the public sector employment, the fiscal devaluation ,defined by the decrease in the consumption and the social security contribution tax rate, recently employed in Germany in 2007, the gradual reduction in the debt ratio from its current value to the Maastricht reference value proposed by Coenen et al.(2008),,the rebate transfer suggested by Kitao (2010), the primary surplus target presented by De Carvalho and Valli (2011). Moreover, Lehmus (2011) suggested many fiscal reforms in Finland. For the instance replacing progressive (labor) with a flat tax (consumption or labor), shifting tax burden from labor to a consumption tax, choosing a policy mix when rising the consumption tax. Also Papageorgiou (2012) suggested a technique in Greece to decrease the higher labor tax. Concerning the limits of this study we can emphasize on the lack of the welfare examination of the policy rule for the household in the same way to Kitao (2010) and Papageorgiou (2012). Also not resorting to the Bayesian estimation inference methods of the NAWM model, as Christoffel et al. (2008) and many other authors, giving the accuracy of this approach. Finally not mentioning the sensitivity analysis tackled by many authors (see Kitao, 2010; Coenen et al. 2008) to check the robustness of some results and better understand how the economy works. For example, when varying the labor supply elasticity of households, or the elasticity of substitution between the home and foreign goods on the macroeconomic variables.

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ANNEXURE

Table 1: Macroeconomic Aggregates (steady state ratios in Tunisia)

Ratio	Value	Description and source
$P_I / P_Y Y$	0.11	http://data.worldbank.org/country/tunisia : the private investment concerns energy, telecom, transport, water and sanitation are calculated on average between 1980 and 2011 then the ratio of private investment / output is calculated
$P_{IM} / P_Y Y$	0.46	(average 1980-2011) source (http://data.worldbank.org/country/tunisia)
$M / (1 + \tau_c) P_c C$	0.21	To calibrate the money-to-consumption ratios, we imputed the fractions of the monetary aggregate M1 held by the household sector over nominal consumption expenditure, the value is obtained is per quarter in Euro Area .In Tunisia we refer to the data obtained from www.bct.gov.tn calculated annually on average.
$P_{IM} / P_Y Y$	0.09	Calculated from http://data.worldbank.org/country/tunisia and IFS.
$B / P_Y Y$	2.30	In Tunisia, it was reported by the central bank from 1990 until 2011 and was averaged to 57, 5%. For the euro area countries the debt-to-output ratio is in line with the «neutral» of the Maastricht reference of $B_Y = 4 \times 57,5\%$ in steady state

Table 2: Calibrated Parameters and Steady State Variables (Household in Tunisia)

Parameter	Value	Description and source
ω	0.53	we refer to a study entitled the "pecuniary resources of a couple and household management "recently realized by the Centre of Research, Documentation and Information on Women (CREDIF), which find that 53% of Tunisian couples recognize that they are not be able to save because they cannot afford

Note: The values of the Euro Area are taken from the previous version of the NAWM of (Coenen et al, 2008), and are not updated given the lack of information on the size of these parameters for the regions of interest

Table 4: Final good firms (in Tunisia)

Parameter	Value	Description and source
u_c	0.49	Calibrated based on IFS data base

Table 6: Fiscal policy

Parameter	Value	Description and source
τ^c	0.29	Source http://data.worldbank.org/country/tunisia average data base From 1990 to 2011(in Tunisia)
τ^N	0.20	Source International Monetary Fund, Government Finance Statistics Yearbook and data files(in Tunisia)
τ^D	0 in Tunisia and Euro Area	In the absence of reliable data, the tax rate on dividend income τ_D is set to zero, while the tax rate on capital income τ_K is determined as a free parameter in the steady-state computation
τ^{Wh}	0.07	http://www.jurisitetunisie.com/tunisie/index/CNSS.htm (calculated on average from 1994 to 2009) (in Tunisia)

Note: Concerning the euro area, data on consumption taxes are standard rates of VAT .Data on labor taxes and social security contributions (in percent of labor cost) are based on single individuals without children at the income level of the average production worker denominated in US dollars with equal purchasing power .The overall tax wedge is defined as the sum of the individual tax wedges. The Euro area average has been calculated using 2004 GDP weights at PPP exchange rates

Table 8: Long run effects consolidation in Tunisia and The Euro Area in%

Parameter	value	Description and source
$\Delta\tau_c$	-0.112	This strategy can be authorized when the government has a lower interest payment on government debt. Economists and politicians generally see that the consumption taxes are the least distortionary way to increase tax revenues collected by the government, or even as a “money machine” for government. The common argument is that consumption taxes do not discourage saving, unlike income taxes (Lehmus, 2011).